# Exam Two , MTH 211, Spring 2010 

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QUESTION 1. Below is a Frieze pattern. State all the symmetries involved in the pattern.

QUESTION 2. Let $D$ be a rectangle $6 \times 3$. We want to remove the line segments that connect the vertices of $D$ and replace them with SOMETHING you select but no line segments are allowed in order to use many pieces of the new object to tile a plane. DRAW ONE IMAGE of the new object that you selected.

QUESTION 3. We want to tile a plane using pieces of regular 8-gon and pieces of another regular n-gon. STATE ALL POSSIBILITIES of the other regular n-gon. JUSTIFY YOUR ANSWER. If $V$ is a vertex of one piece of a regular 8-gon, How many pieces of regular 8-gon and how many pieces of the other regular n-gon share the vertex $V$

QUESTION 4. Define the concept of similarity of a plane.

Define the concept of Central similarity of a plane.

Let $f: R^{2} \rightarrow R^{2}$ be a CENTRAL similarity of the plane $R^{2}$. Given if $D$ is a square in the plane with perimeter equals to 16 cm , then after applying $f$ on $D$ we get a square $D \prime$ (i.e. $f(D)=D \prime$ ) that has a perimeter equals to 4 cm .
a) Let $M$ be a $12 \times 8$ rectangle in the plane. Find the length and the width of $M I=f(M)$ (i.e. Find the length and the width of the new rectangle $M \prime$ after applying $f$ on $\mathbf{M}$ )
b) Let $z=(-4,20)$ find $\mathrm{f}((-4,20))$.

QUESTION 5. Construct a line segment ab of length 3 cm . Now construct a circle $C$ with radius 5 such that $C$ passes through $a$ and $b$. If $\operatorname{Inv}(\mathrm{ab})$ with respect to $C$ is a line segment, then find the exact length of the line segment $\operatorname{Inv}(\mathrm{A}) \operatorname{inv}(\mathrm{B})$. If $\operatorname{Inv}(\mathrm{ab})$ with respect to $C$ is an arc, then DRAW THE EXACT ARC that equals to $\operatorname{Inv}(\mathrm{ab})$.

QUESTION 6. Draw the inversion of $D$ with respect to the circle $C$.

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